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Theoretical basics and modern status of radioactivity studies

Lecture 2: Radioactivity

# Coefficients

$$\hbar = c = 1$$

$$1 \text{ ns} \rightarrow 30 \text{ cm}$$

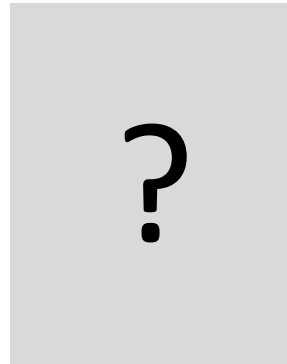
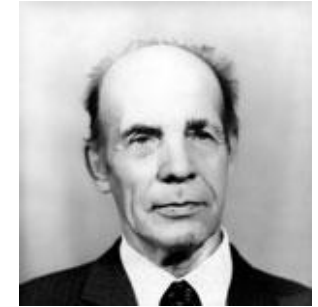
$$1 \text{ year} = \pi \times 10^7 \text{ s}$$

$$\Gamma [\text{MeV}] = \frac{4.56 \times 10^{-22} [\text{MeV s}]}{T_{1/2} [\text{s}]}$$

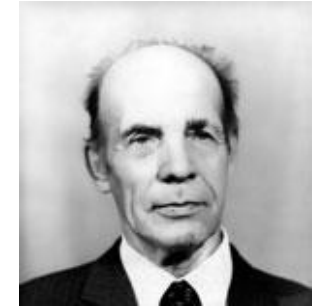
$$\frac{[\text{MeV}][\text{fm}]}{197.327}$$

<b>E (AMeV)</b>	<b>v</b>	
5	0.103	<b>Coulomb barrier</b>
20	0.203	<b>Intermediate</b>
100	0.428	<b>energies</b>
1000	0.875	<b>Relativism</b>

# Radioactivity “hall of fame”



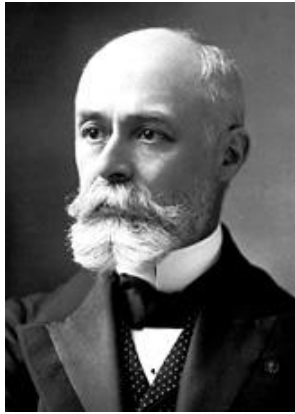
# Radioactivity “hall of fame”



**Henri Becquerel:** three types of radioactivity - negative, positive, and electrically neutral



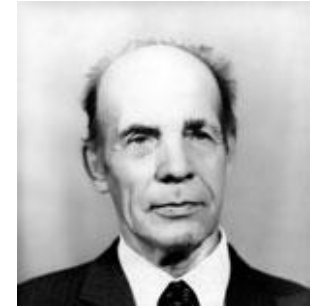
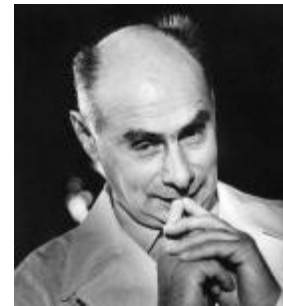
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Henri Becquerel: three classes of radioactivity - negative, positive, and electrically neutral



F. Joliot and I. Curie:  
 $\beta^+$



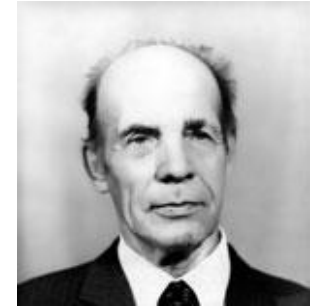
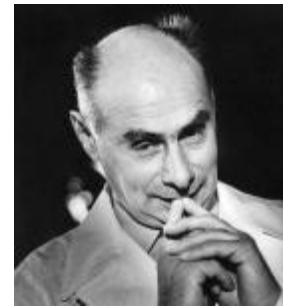
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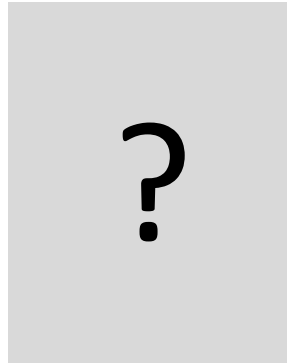
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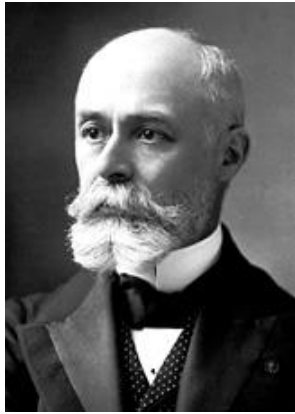
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G.N. Flerov and K.A. Petrzhak  
spontaneous fission



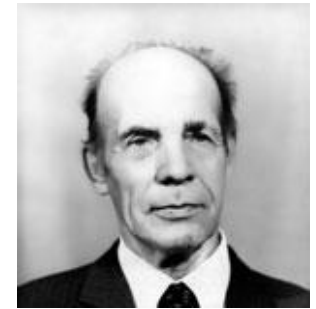
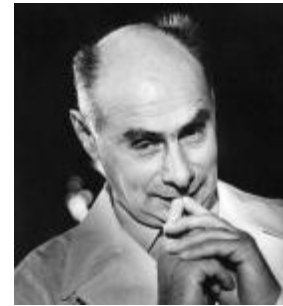
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G.M. Ter-Akopian  
 $\beta$ -delayed p



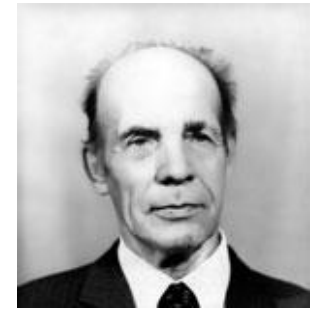
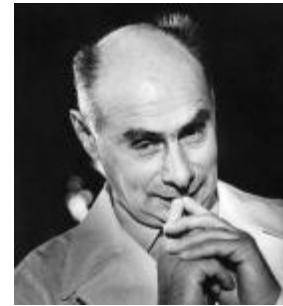
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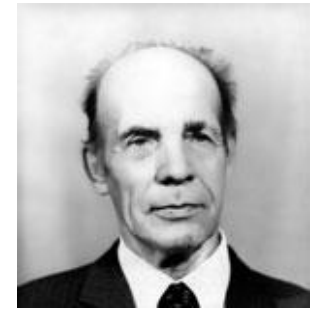
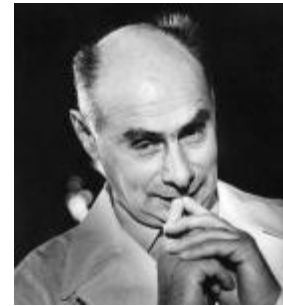
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M. Pfützner:  
2p



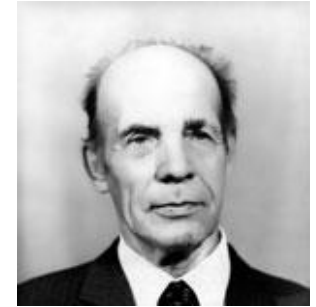
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???  
2n radioactivity

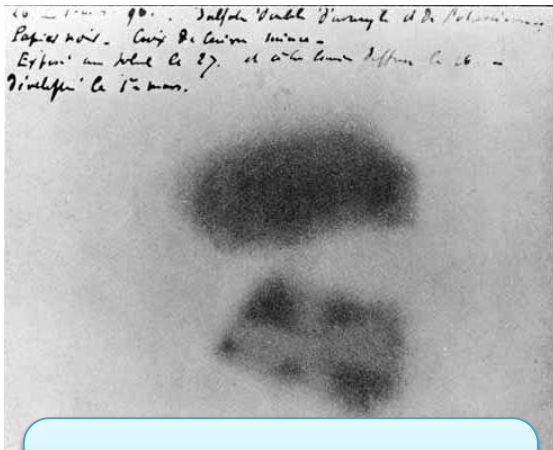


???  
4n radioactivity

# Discovery of radioactivity 1896. Classical era of radioactivity



**Henri Becquerel:** three classes of radioactivity - negative, positive, and electrically neutral



**Becquerel** Bq  $1 \text{ s}^{-1}$   
**Curie**  $1 \text{ Ci} = 3.7 \times 10^{10} \text{ Bq}$

Polonium and Radium, Curie and Curie, 1898

$\alpha$  and  $\beta$  rays distinguished by Rutherford, 1899

$\gamma$  rays distinguished by Villard, 1900

Atomic nucleus, Rutherford, 1911

Explanation of  $\alpha$  decay, Gamow, 1928

Theory of  $\beta$  decay, Fermi, 1934

$\beta^+$  decay discovered by Curie and Joliot, 1934

Electron capture Wick, Bethe, and Peierls, 1934

Spontaneous fission, Flerov and Petrzhak, 1940

# Impact of radioactivity discovery on the philosophical worldview



**What was most important in the discovery of radioactivity?**

# Impact of radioactivity discovery on the philosophical worldview



**Classical physics: world of cause and consequence**

**Key word: spontaneous**

**Difficult to imagine nuclei as tiny clockworks counting the time up to decay moment**

**Paving way for quantum vision of the physical world**

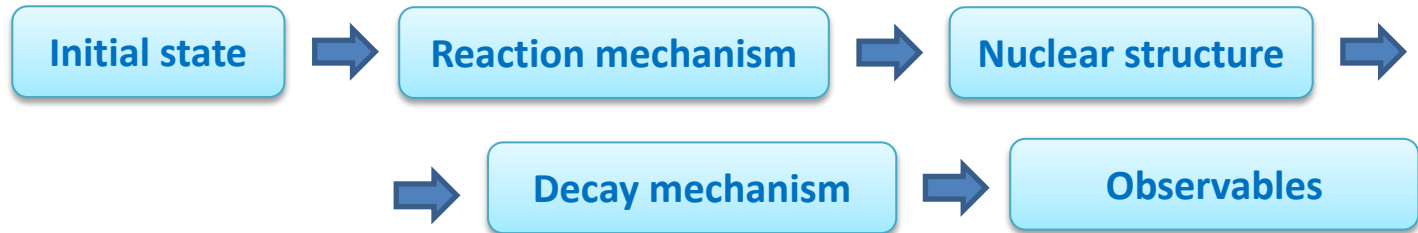
**These people were to be very open-minded and critical to themselves to overcome the scientific challenge of their epoch. Our times are different – we do not feel that next scientific revolution is close. Could be true. Could be not true. However, lesson to us to be not less creative...**

# Why to study radioactive decays

**“Active” vs “passive” approach**

**Reactions**

Choice of reaction can be very selective for the question of interest



**Decays**

Decay provide only one type of information



**It decay studies there are fewer steps from observables to valuable information**

**Reaction theory is very fuzzy as any strong interaction theory (electron scattering is exception)**

**Decay mechanism (final state interactions) could be accessible for very precise theoretical investigation**

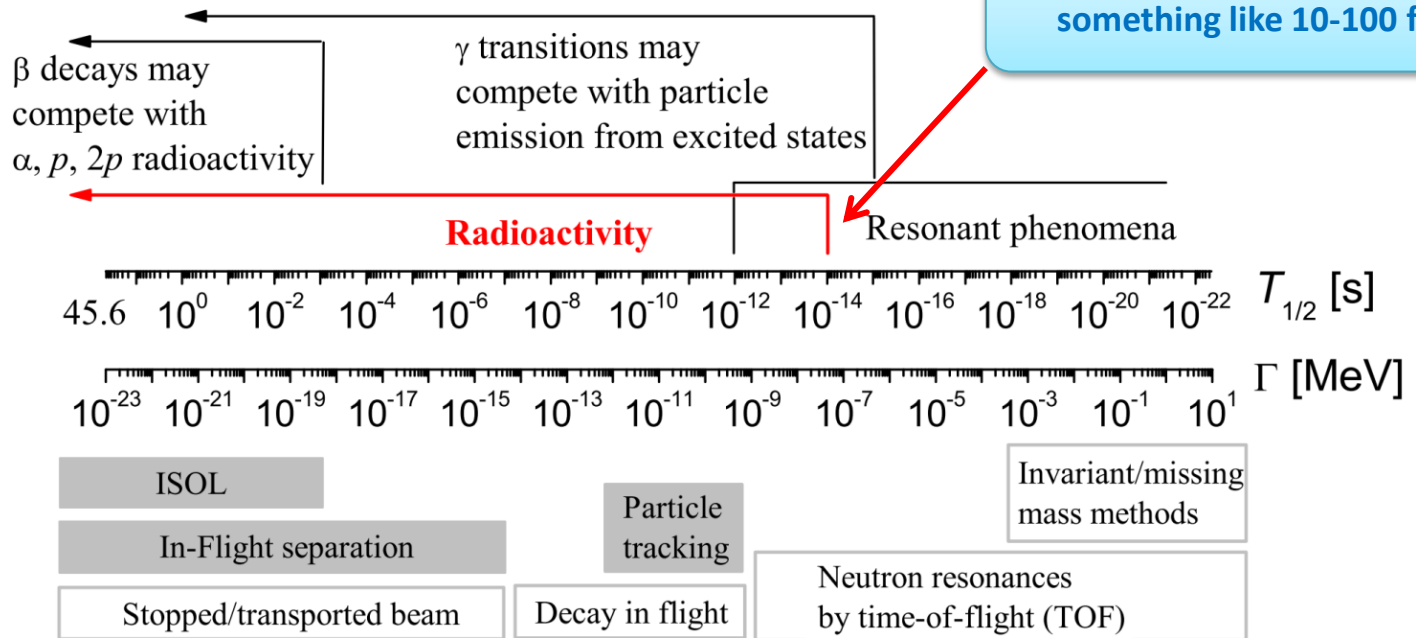
# Time scales

**Initial idea: radioactivity is process when something is radiated**

“Atom” in the definition means that process is slow enough that atom (electronic orbitals) can be formed.

**Modern definition: energy loss by atom**

No absolutely strict value, but something like 10-100 fs...



**Extremely broad lifetime scale – 25 orders of the magnitude**

**Qualitatively different experimental techniques**

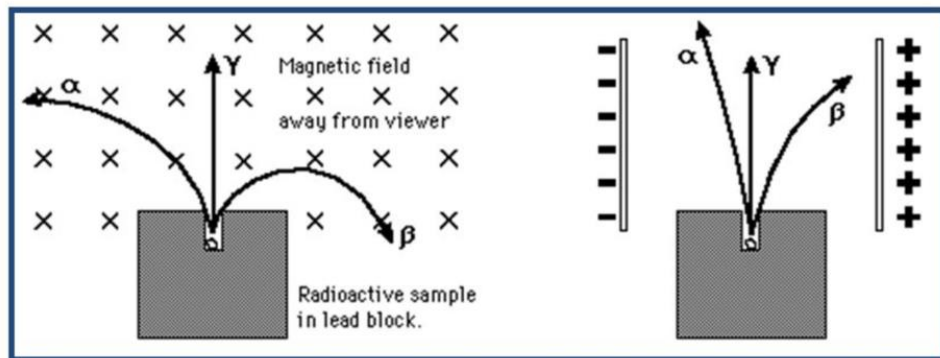
1 sec vs. Universe lifetime – 17-18 orders of the magnitude

Where the decay is taking place





# Types of radioactivity: since 1896



	Interaction domain	Decay suppression reason
Alpha	Strong	Electromagnetic
Beta	Weak	Coupling constant
Gamma	Electromagnetic	Strong

# Types of radioactivity: isomers

Typical gamma-decay lifetime is in fs range.  
However, there exist very slow gamma transitions

Definition of isomeric state:  $T_{1/2} > 10^{-9}$  s  
– if you produce it in some reaction, the isomer survive long enough to be spatially separated from production target

Classical example  $^{180m}\text{Ta}$

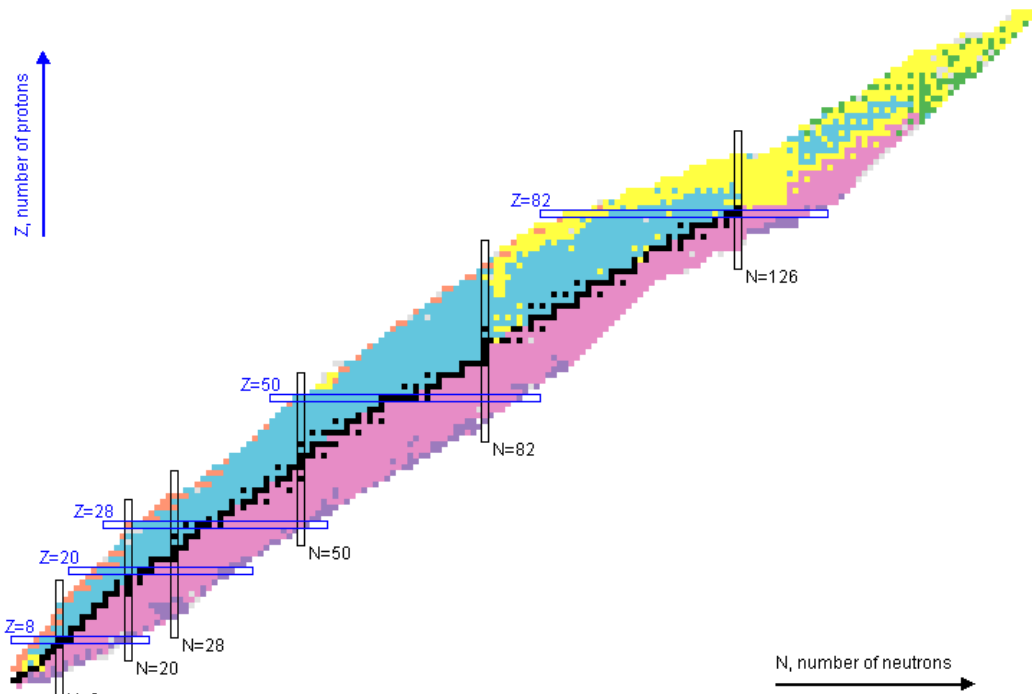
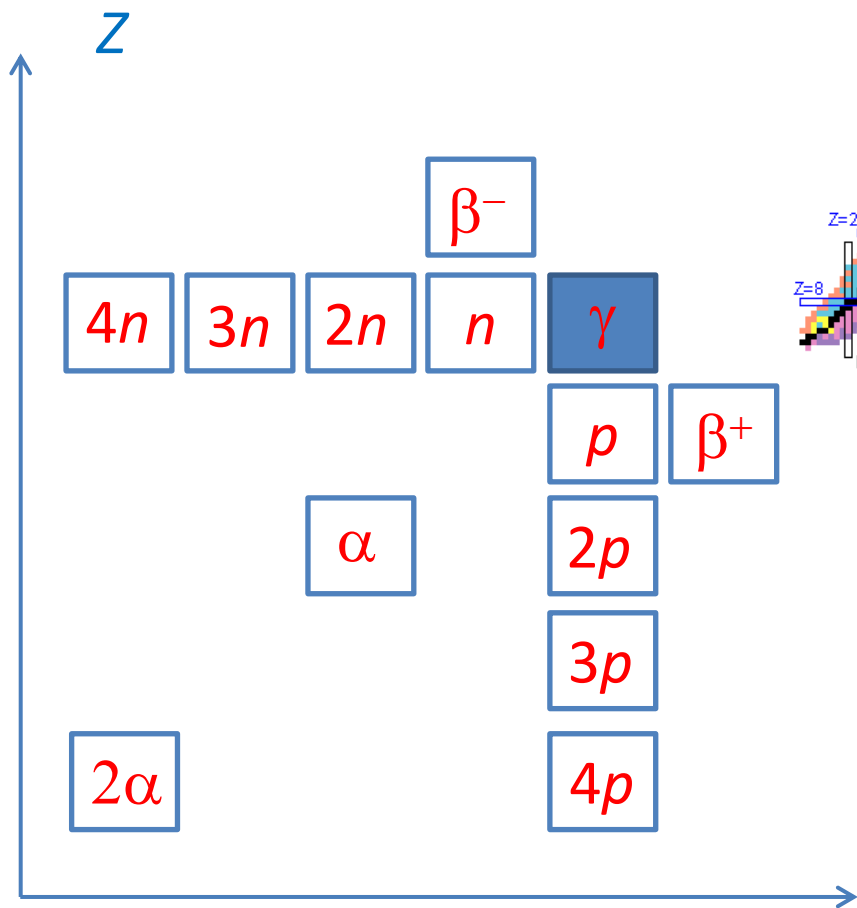
$^{180}\text{Ta}$  is abundant in nature ( $< 0.01\%$ )

	$E^*$ (MeV)	$J^\pi$	$T_{1/2}$
$^{180}\text{Ta}$	0	$1^+$	8 hours
$^{180m}\text{Ta}$	0.07	$9^-$	$>10^{15}$ years

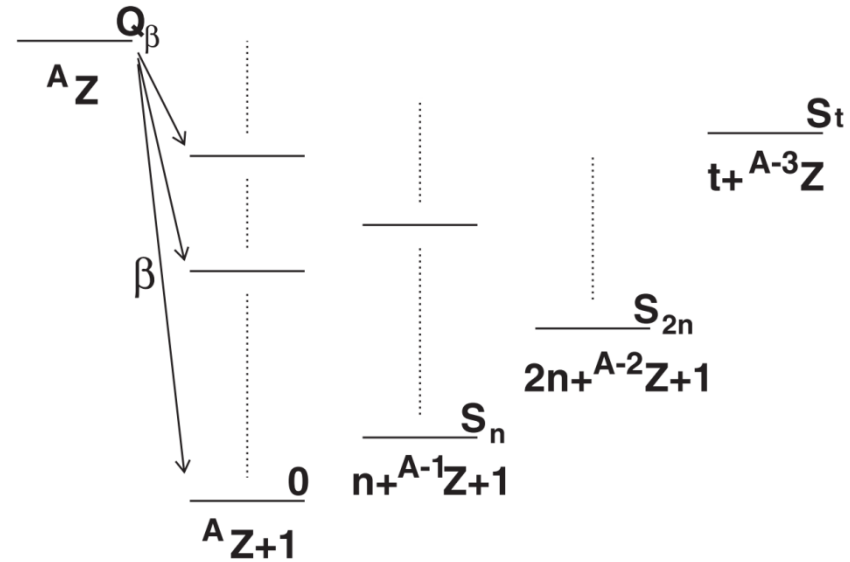
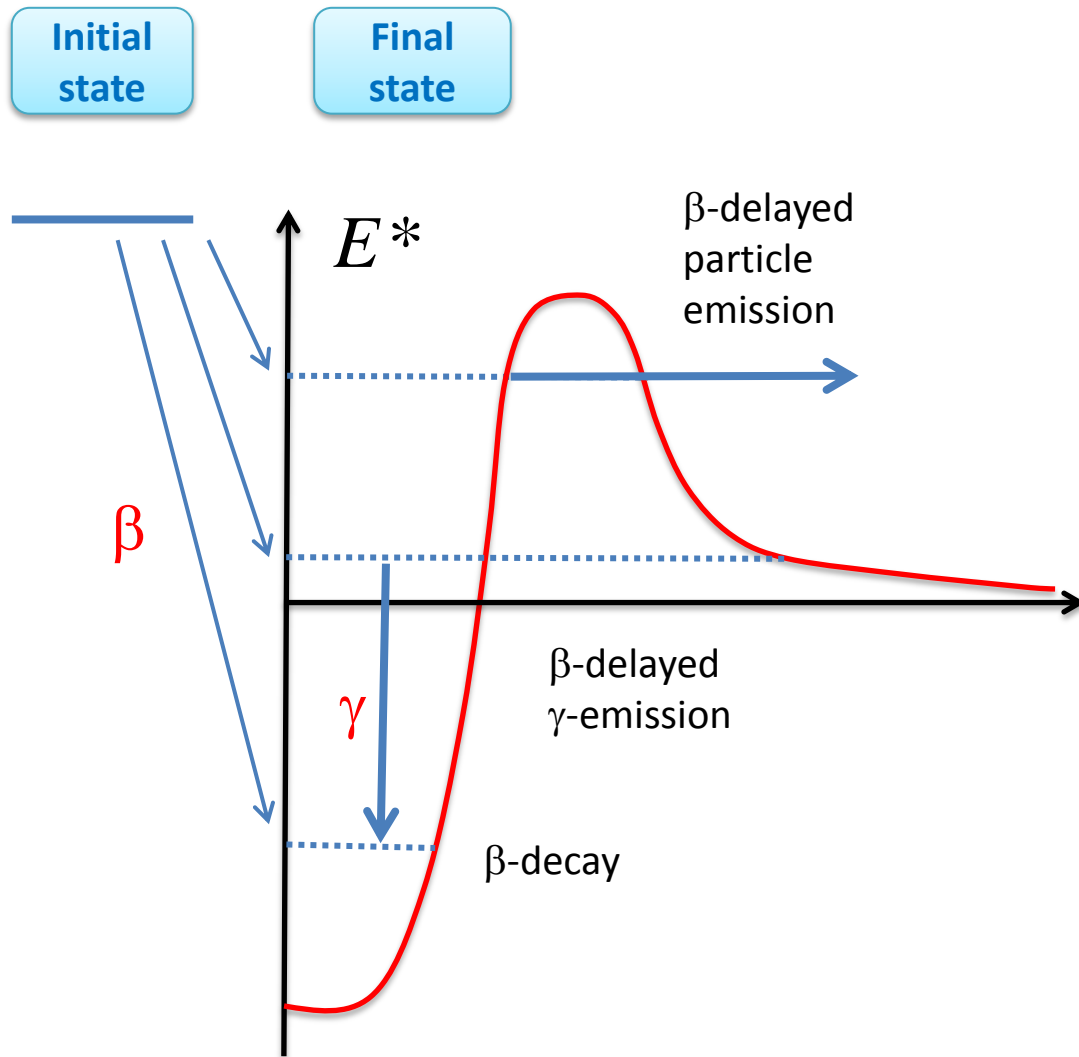
So, all  $^{180}\text{Ta}$  isotope is in isomeric state which has survived since secondary nucleosynthesis in our galaxy

# Types of radioactivity: more details

Transmutation networks in the map of nuclides

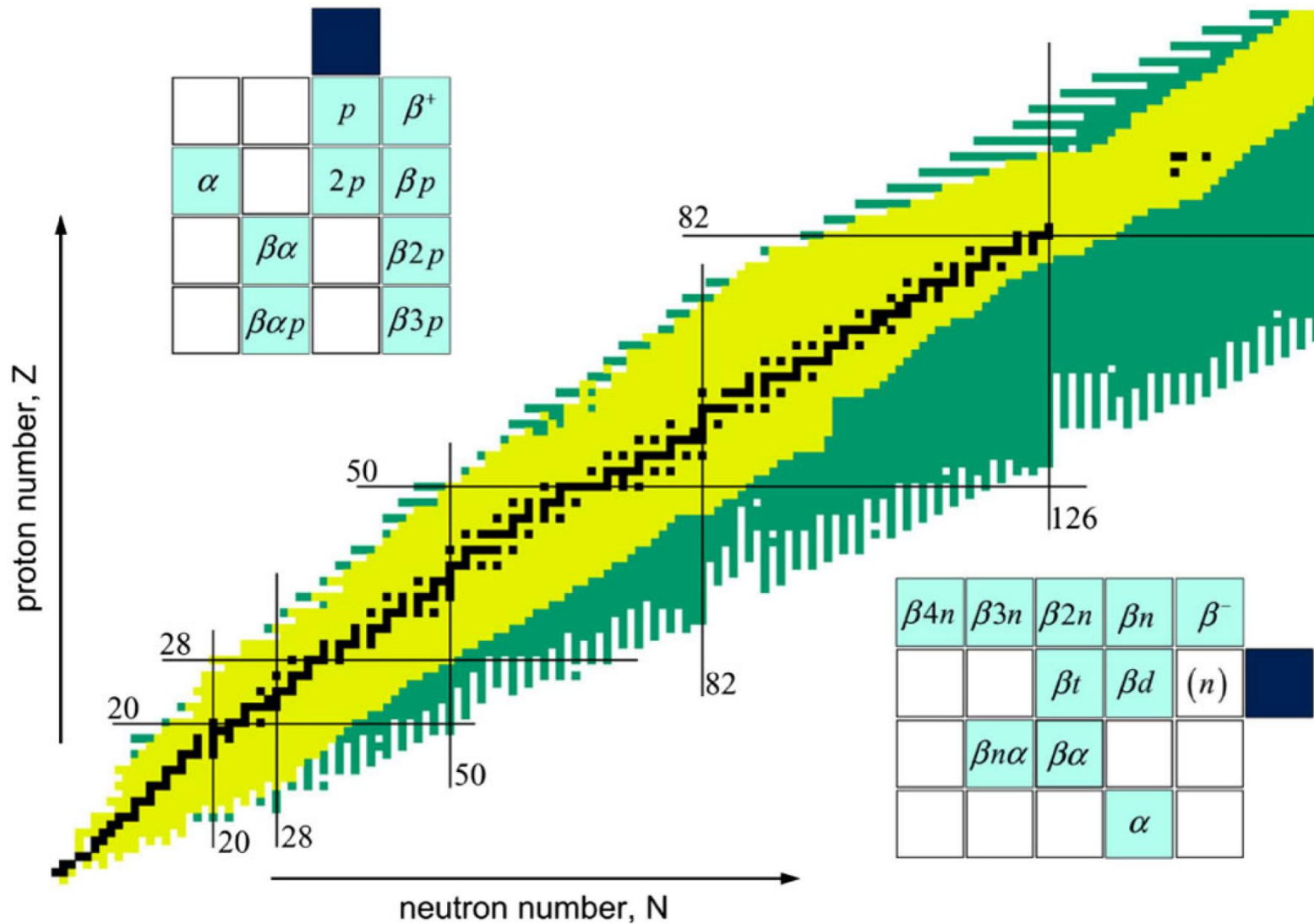


# Types of radioactivity: $\beta$ -delayed particle emission

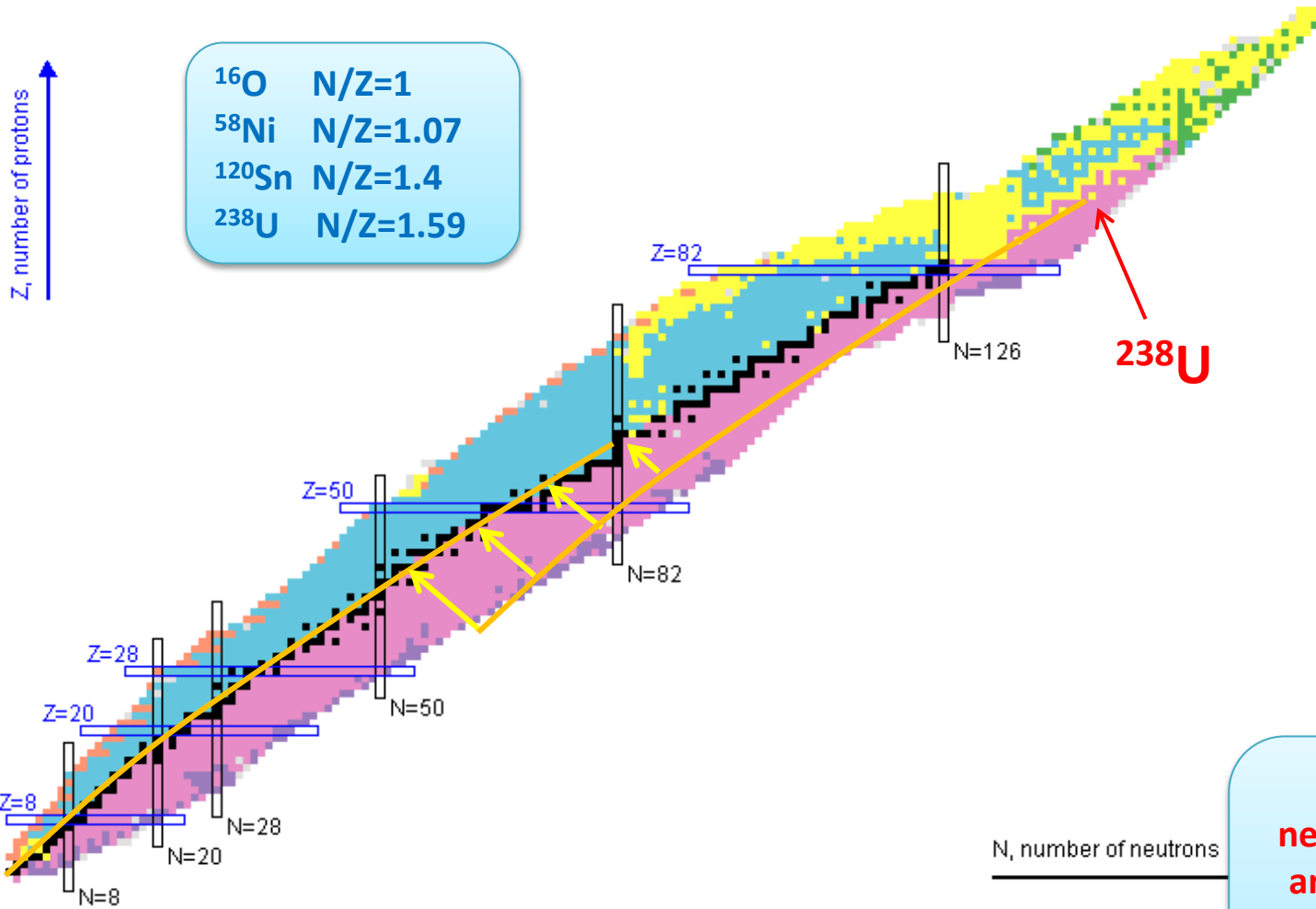


If emitted particle is well excited or particle-unstable we get to situation of multi-particle emission

# Types of radioactivity: $\beta$ -delayed particle emission



# Types of radioactivity: spontaneous fission



Heavy nuclides are increasingly neutron excessive

Fission resulting in stable nuclides is unlikely

Fission resulting in ground state is unlikely

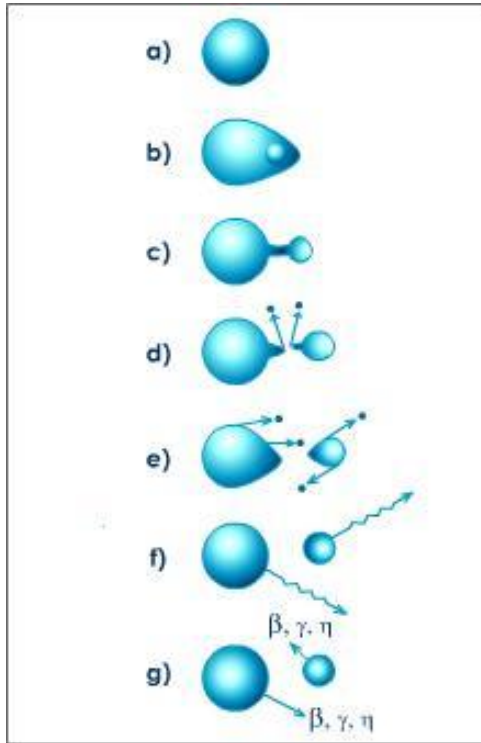
Excited states of neutron-rich nuclides are populated. They discharge by sequence on gamma, beta and neutron decays

Source of delayed neutrons to enforce induced fission in nuclear reactors

N, number of neutrons



# Droplet model of nucleus. Bethe–Weizsäcker formula



$$E_B = a_V A - a_S A^{2/3} - a_A \frac{(A-2Z)^2}{A^{1/3}} - a_C \frac{Z(Z-1)}{A^{1/3}} + \delta(A, Z)$$

Volume  
term

Surface  
term

Asymmetry  
term

Coulomb  
term

Pairing  
term

For pairing term:

$$\delta(A, Z) = \begin{cases} +\delta_o & A, Z \text{ even} \\ 0 & A \text{ odd} \\ -\delta_o & A, Z \text{ odd} \end{cases}$$

where

$$\delta_o = \frac{a_p}{A^{1/2}}$$

Coefficients:

$$a_V = 15.85 \text{ MeV}$$

$$a_S = 18.34 \text{ MeV}$$

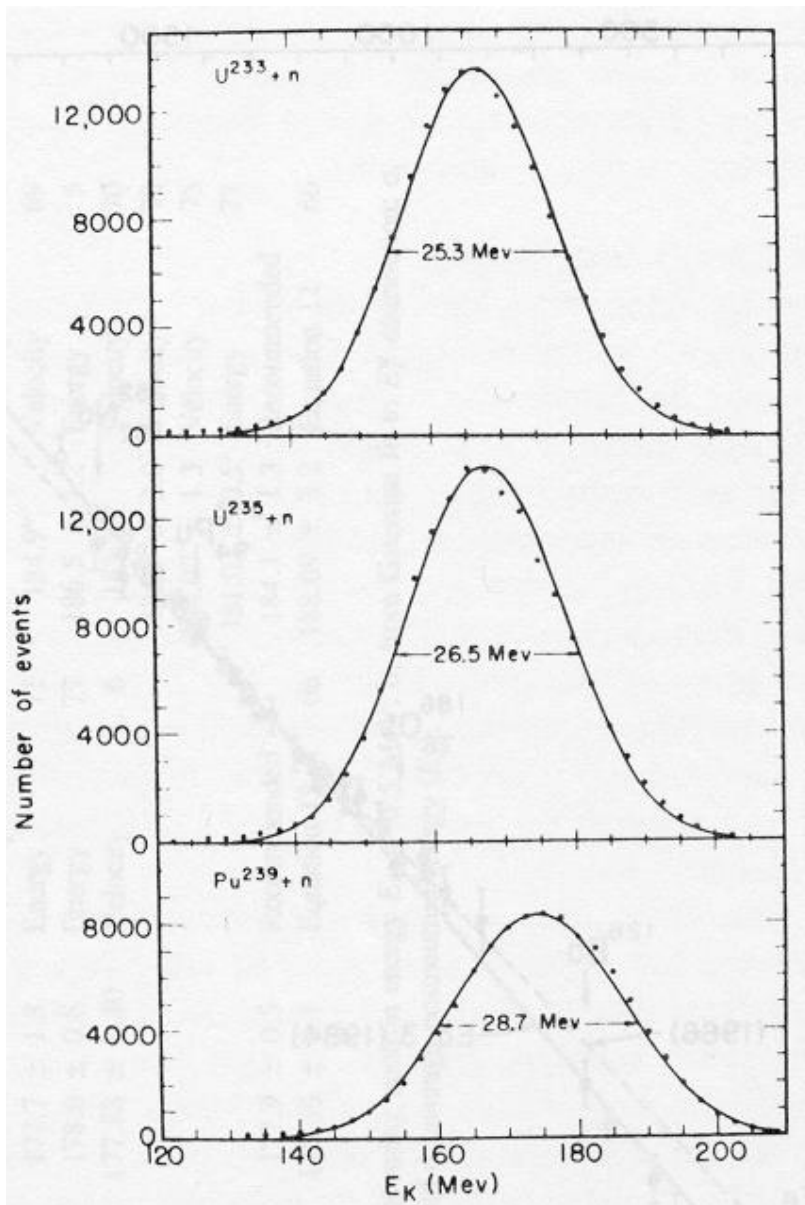
$$a_A = 23.21 \text{ MeV}$$

$$a_C = 0.714 \text{ MeV}$$

$$a_p = 12.00 \text{ MeV}$$

- Substance with saturated density - liquid
- Liquid droplet model of nucleus
- Fission physics: analogy with charged droplet instability
- Simple mass relations: Bethe-Weizaecker formula

# Energy release in fission



**Up to 240 MeV per fission**

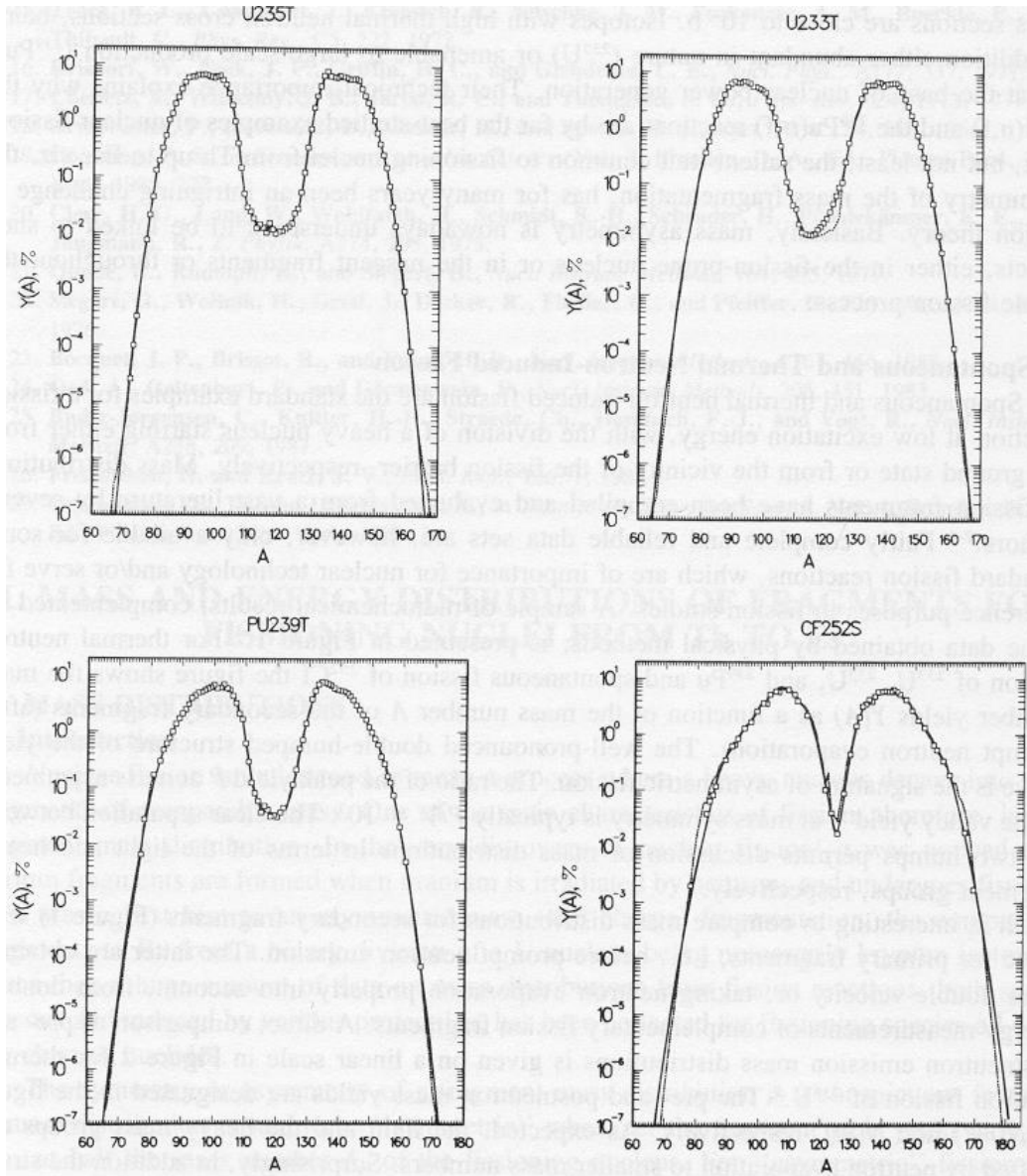
**From 150-200 MeV per fission  
is due to electrostatic energy  
released via kinetic energy of  
fragments**

TKE distribution for fission fragments before secondary neutrons are emitted



# Fragment mass distribution in fission

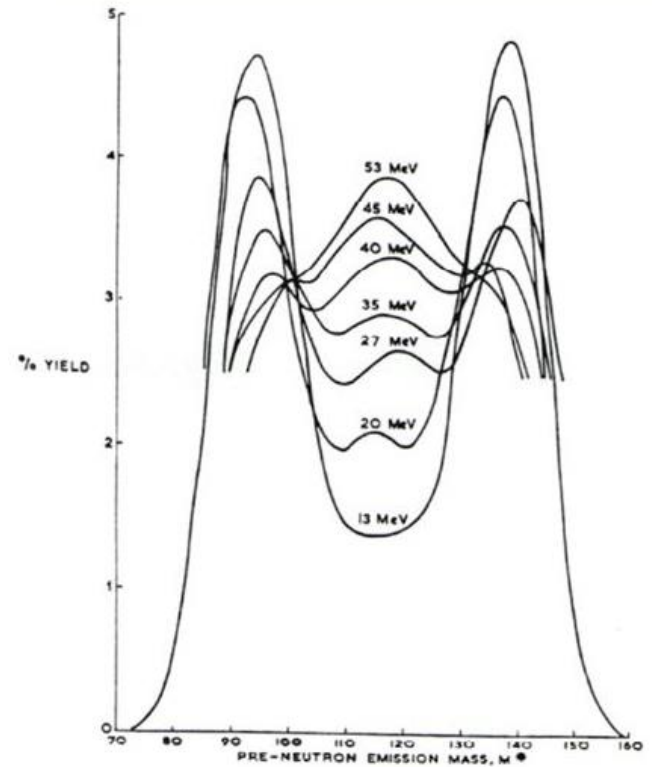
**Asymmetric fission is the most typical fission mode**



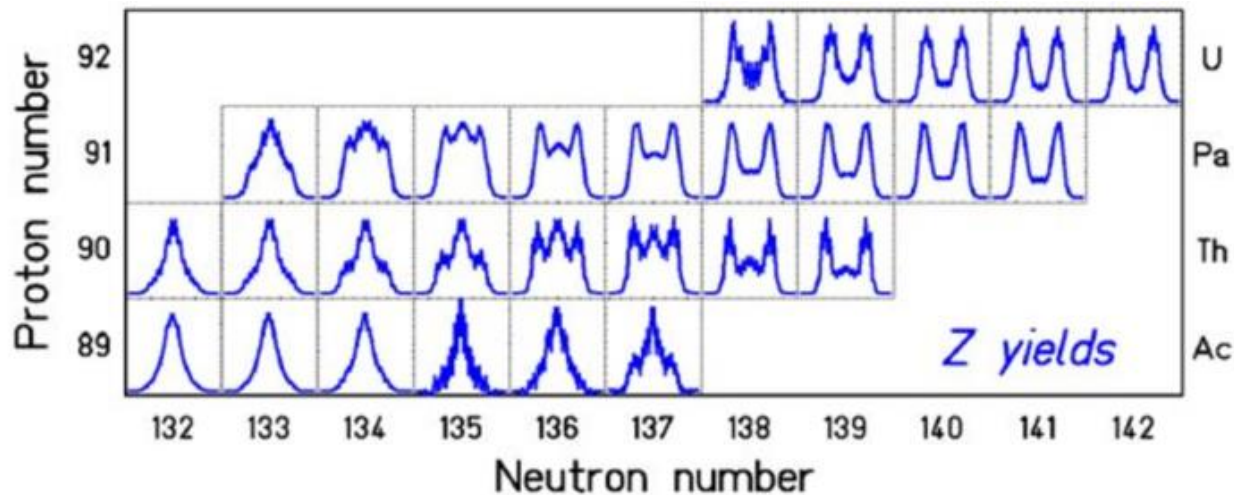
# Fragment mass distribution in fission

Induced fission is increasingly symmetric with energy increase of inducing particle

Transition from asymmetric to symmetric fission takes place in exotic nuclides

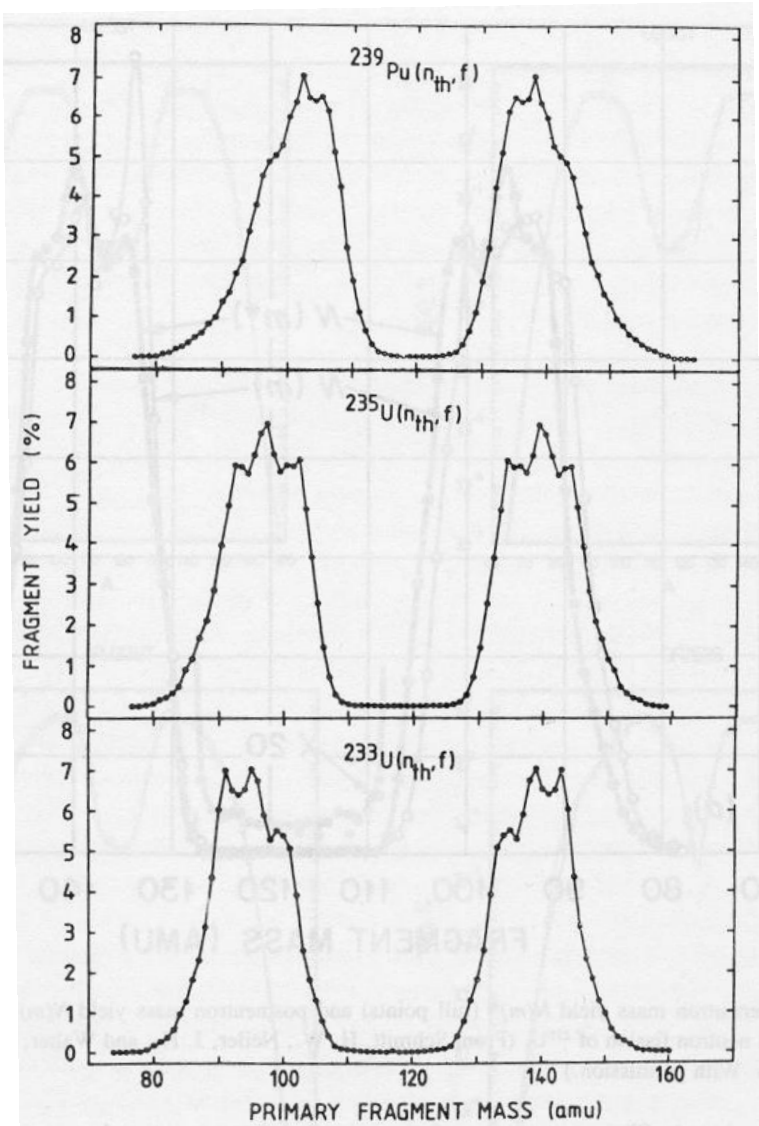


Fission mass distributions for  $^{232}\text{Th}(p, f)$

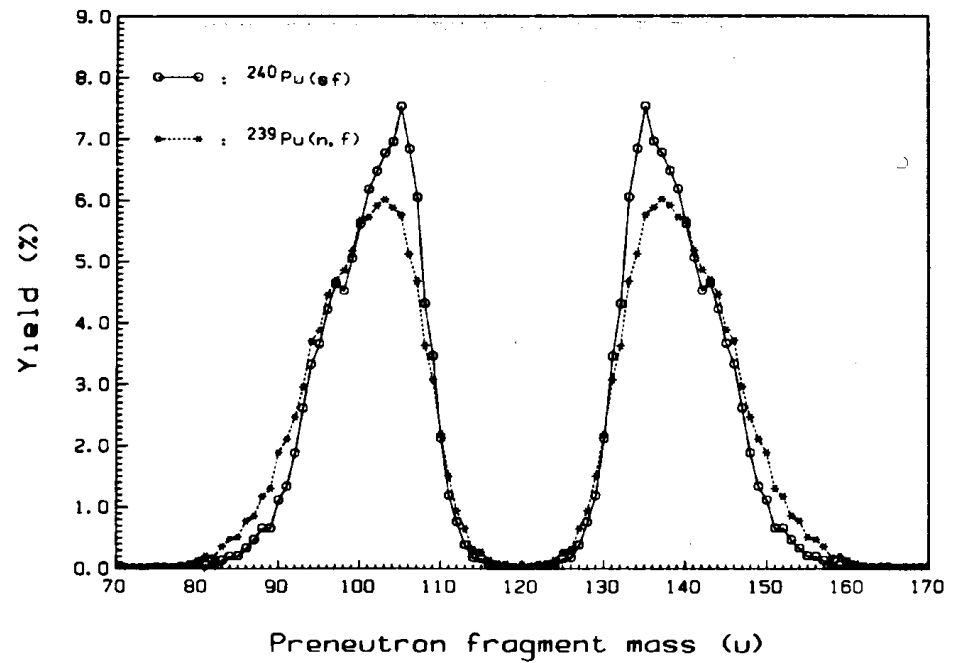


# Fine structure of fission fragments mass distribution

Mass spectra of fission fragments before prompt neutron emission



Fine structure of mass spectra of fission fragments is enhanced in spontaneous fission



# Proton radioactivity

Goldansky, 1960 1960, Nucl. Phys. 19, 482.

**“Modern era” of radioactivity studies:**

- Proton radioactivity
- Beta-delayed proton emission
- Two-proton radioactivity



Nothing special compared to alpha emission. However, shift of interest to the systems near the proton dripline and beyond

**Beta-delayed proton emission discovery**

$^{17}\text{Ne}$  Karnaukhov, Ter-Akopian, Subbotin, 1963

$^{25}\text{Si}$  Barton et al., 1963



**Proton radioactivity discovery**

$^{53\text{m}}\text{Co}$  proton emission off isomeric state  
Jackson et al., 1970.

$^{151}\text{Lu}$  ground-state proton radioactivity  
Hofmann et al., 1982

**Now proton radioactivity is well studied**

**~50  $s=1$  odd mass cases from  $^{109}\text{I}$  to  $^{185}\text{Bi}$**

**17  $s=2$  even mass cases from  $^{112}\text{Cs}$  to  $^{176}\text{Tl}$**

**3  $s>2$  cases:  $^{53\text{m}}\text{Co}$ ,  $^{54\text{m}}\text{Ni}$ ,  $^{94\text{m}}\text{Ag}$**

# Types of radioactivity: cluster radioactivity

Natural generalization: p, alpha, heavier than alpha?

## Predictions

A. Sandulescu, D.N. Poenaru, and W. Greiner, 1980

## Cluster radioactivity discovery

$^{17}\text{Ne}$  from  $^{223}\text{Ra}$ , Rose and Jones, 1984

Unprobable process:  
branching ratio to alpha  
emission  $< 10^{-5}$ ,  
typical:  $10^{-12}$ - $10^{-15}$

~ 36 cases

$^{12}\text{C}$  from  $^{114}\text{Ba}$



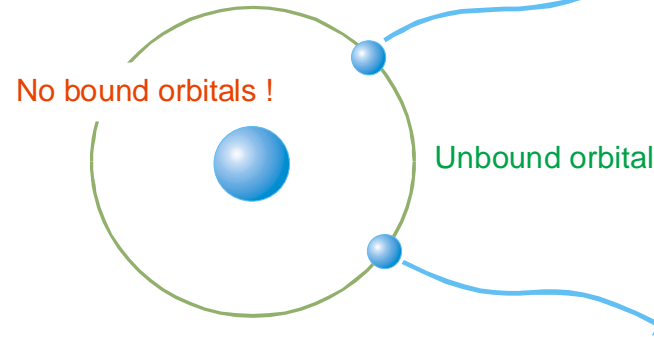
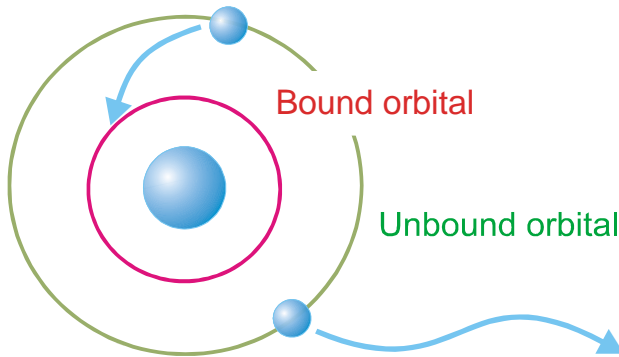
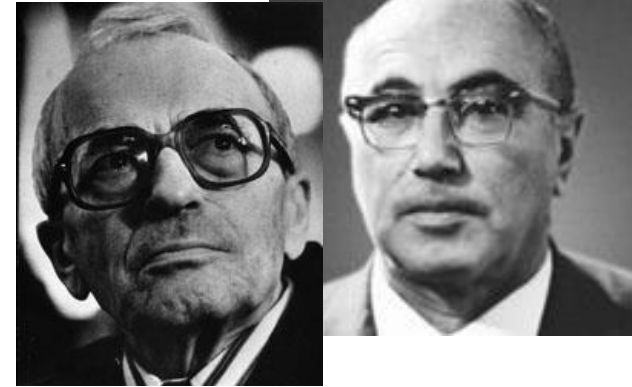
$^{34}\text{Si}$  from  $^{242}\text{Cm}$

$^{12,14}\text{C}$ ,  $^{20}\text{O}$ ,  $^{23}\text{F}$ ,  $^{22,24-26}\text{Ne}$ ,  $^{28,30}\text{Mg}$ ,  $^{32,34}\text{Si}$   
Mainly even mass closed-shell clusters are emitted

Where is borderline  
between cluster  
radioactivity and fission?

The decay via ground or  
lowest excited states of  
daughter systems

# Two-proton radioactivity: a qualitative view



Goldansky and  
Zeldovich, 1960

Pfutzner et al and  
Giovinazzo et al, 2002

Classical case:  
one particle emission is always possible

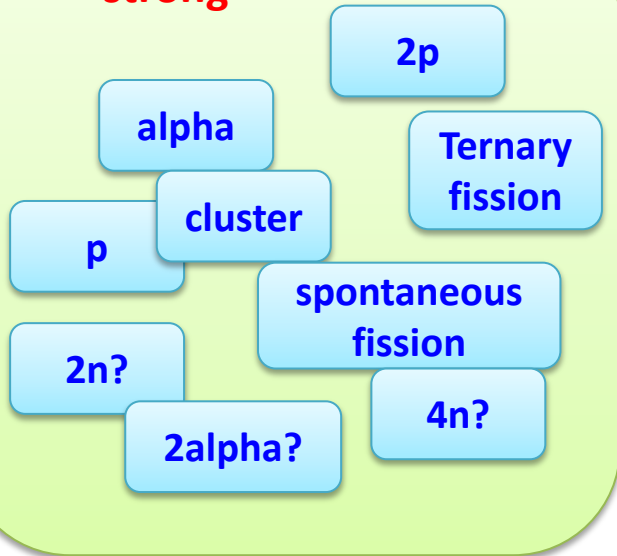
Quantum mechanical case:  
it could be that both particles should  
be emitted simultaneously

**Exclusive  
Quantum-  
Mechanical  
phenomenon**

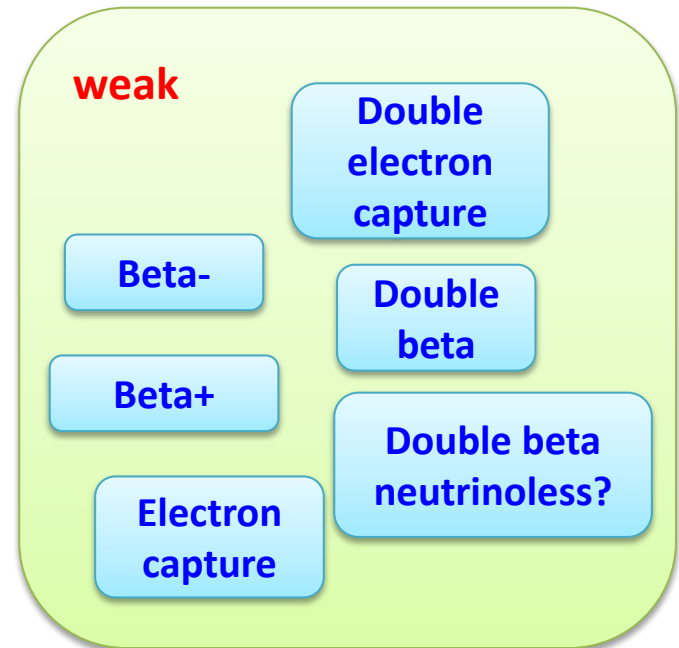
- **No deeper bound orbitals.**
- **The common orbital for two protons exists only when both are “inside”.**
- **When one of them goes out, their common orbital do not exist any more and the second HAS to go out instantaneously**

# Radioactivity

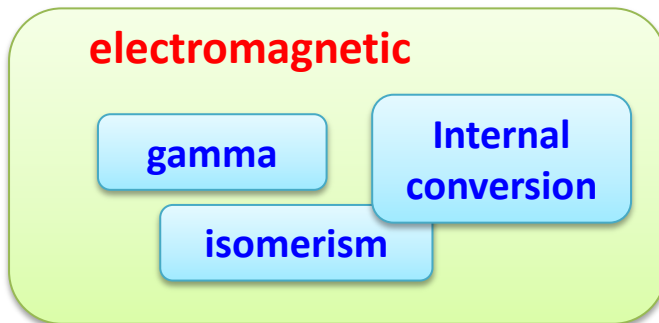
## strong



## weak



## electromagnetic



## Beta-delayed

